

[https://classroom.github.com/a/YOMi\\_a\\_j](https://classroom.github.com/a/YOMi_a_j)

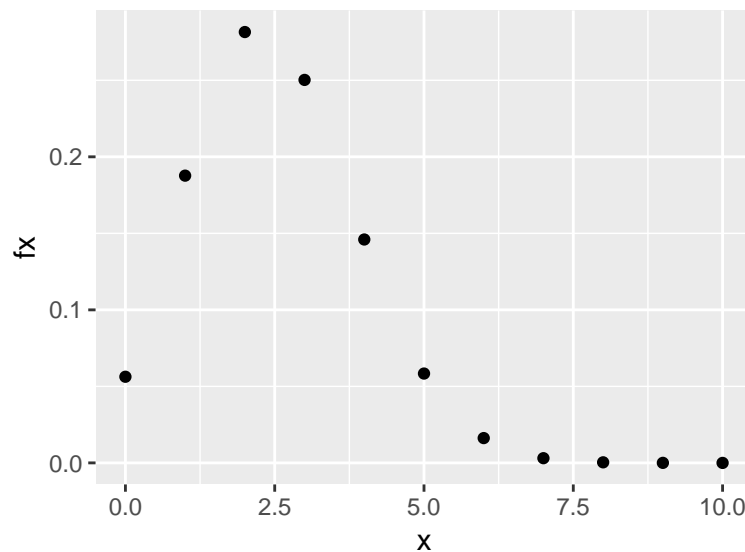
Assume  $X_1, \dots, X_N \sim_{iid} \text{Poisson}(\lambda)$ . The Poisson probability density function is

$$f(x|\lambda) = \frac{e^{-\lambda} \lambda^x}{x!}$$

for  $x \in \mathbb{N}$ .

1. Plot the probability density function for a Poisson distribution. The code I used for the binomial distribution is below.

```
suppressMessages(library(tidyverse))
df <- tibble(x = 0:10, fx = dbinom(x, 10, 0.25))
ggplot(df, aes(x, fx)) + geom_point()
```



```
## hint: ?dpois
```

2. Find the maximum likelihood estimator of  $\lambda$ , that is the best guess of the unknown population parameter  $\lambda$  based on the data  $\mathbf{X}$ . Call your estimator  $\hat{\lambda}$ . Show your work by typing out the appropriate  $\text{\LaTeX}$ .
3. Randomly sample  $N = 1001$  random Poisson variables with your choice of  $\lambda$ , and store it into a variable named  $\mathbf{x}$ .
4. Use your maximum likelihood estimator to estimate  $\lambda$ , based on your randomly sampled data  $\mathbf{x}$ .