

- 9 (a)  $d = \int_1^\infty y^{-3} dy = \left. \frac{-y^{-2}}{2} \right|_1^\infty = 1/2 \Rightarrow d = 2.$   
 (b)  $\mathbb{E}(X) = \int_1^\infty 2y^{-2} dy = \left. -2y^{-1} \right|_1^\infty = 2$   
 (c)  $\mathbb{E}(X^2) = \int_1^\infty 2y^{-1} dy = \log y \Big|_1^\infty \rightarrow \infty$  and hence, the variance is not finite.
- 12 Note that  $\mathbb{E}(X) = M'(0)$ ,  $\mathbb{V}(X) = \mathbb{E}(X^2) - \mathbb{E}(X)^2 = M''(0) - M'(0)^2$ , and that  $M(0) = 1$ .
- (a)  $R'(0) = M'(0)M(0)^{-1} = M'(0)$   
 (b)  $R''(0) = M''(0)M(0)^{-1} - M'(0)M(0)^{-2}M'(0) = M''(0) - M'(0)^2$
- 18 This is easiest if we first find the Cumulative Distribution Function.  $F(x) = \int_{-1}^x (s + 1)/2 ds = (s + 1)^2/4 \Big|_{-1}^x = (x + 1)^2/4$ .  $\pi_p$  is found by solving for  $x$  in  $F(x) = \pi_p$ .

```
2*sqrt(.64) - 1 # a
```

```
## [1] 0.6
```

```
2*sqrt(.25) - 1 # b
```

```
## [1] 0
```

```
2*sqrt(.81) - 1 # c
```

```
## [1] 0.8
```